



Electrokinetic assembly and manipulation II

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1



Outline

- Electroosmosis in particle manipulation
- Micro/nano fluidics with an electric field
- Size exclusive capture using nanoneedles

2

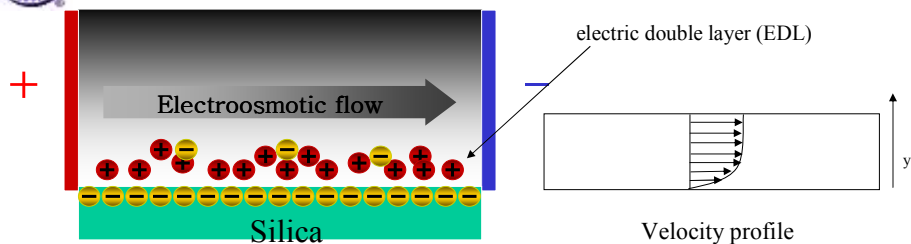


Electroosmosis in particle manipulation

3



Electroosmosis



Patankar et al., Analytical chemistry, 1998

$$\rho \dot{\mathbf{v}} = -\nabla p + \mu \nabla^2 \mathbf{v} + \rho_E \mathbf{E}$$

$$\nabla^2 \phi = -\rho_E / \epsilon \Rightarrow \nabla^2 \phi = \kappa^2 \phi$$

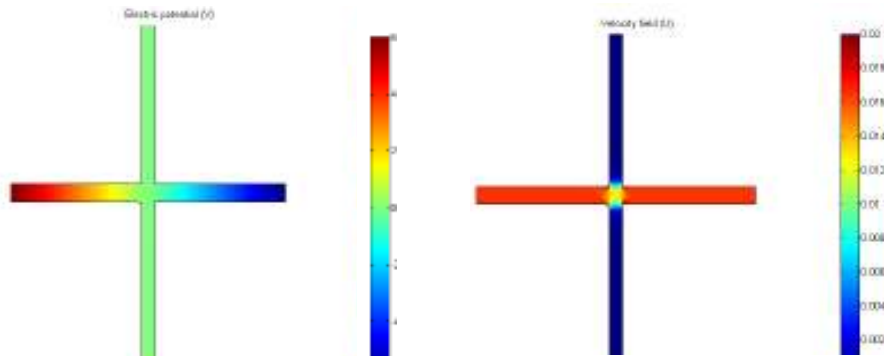
EDL is very thin (a few nm), a slip boundary
can be used at the electrode surface:

$$u_s = -\frac{\epsilon \psi_0 E_x}{\mu}$$

4



Electroosmotic flow



the distribution of electric field potential

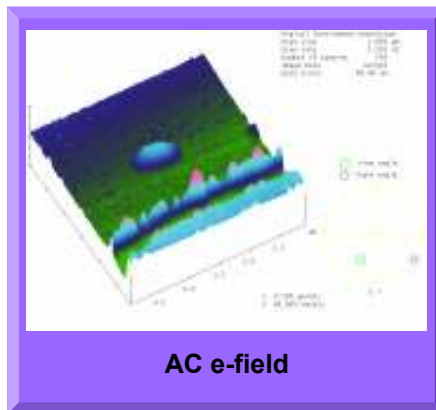
flow velocity in the channel

- Simulation of electroosmotic flow in a cross-sectional fluid channel

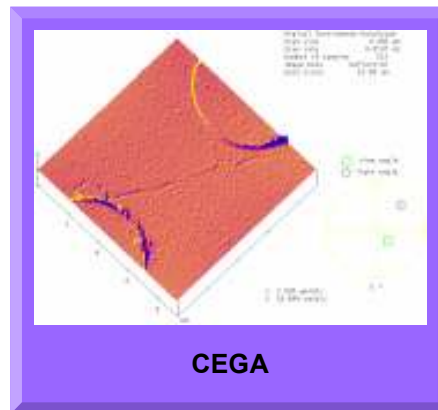
5



Electroosmotic flow



AC e-field



CEGA

- DNA under an AC field and a composite field.
- Electroosmotic flow by the DC field stretches DNA.
- Deposition at 100°C from 1aM solution (about 70 molecules in 150 μ L.)

6



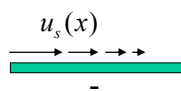
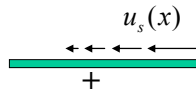
AC electroosmosis flow



The charge relaxation time of a liquid: $\tau = \epsilon / \sigma$ ϵ, σ are fluid permittivity and conductivity

- If the AC frequency $f < 1/(2\pi\tau)$, charge on electrodes and in EDL alternates according to potential sign change
- The flow direction doesn't change with potential sign change

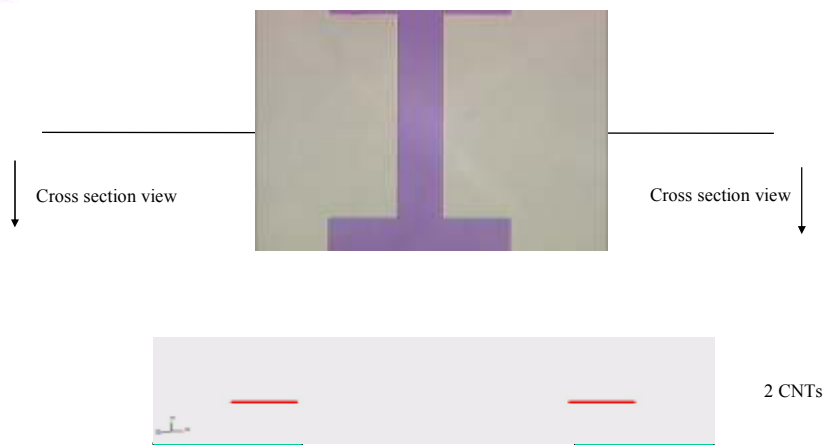
$$u_s = -\frac{\epsilon \psi_0 E_x}{\mu}$$



7



Rotation induced by local electroosmosis flow



AC field 100 Hz, $0.5\text{V}/\mu\text{m}$, parallel electrodes gap size: $5\text{ }\mu\text{m}$
Local electroosmosis flows near the edges of electrodes induce vortices and lead to CNTs rotation

8



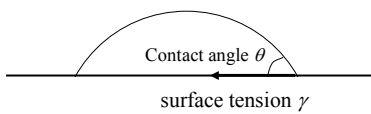
- **Micro/nano fluidics**
- **with an electric field**

9

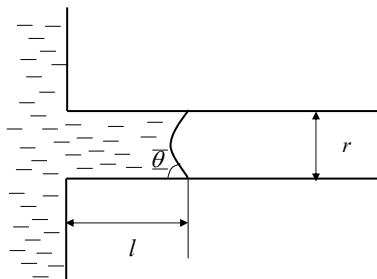


Capillary filling

- Dynamics of capillary filling without ionic effect



Pressure from surface tension $p_c = \frac{2\gamma \cos(\theta)}{r}$



Washburn equation $\frac{dl}{dt} = \frac{(P + P_c)r^2}{8\mu l}$

When external pressure $P=0$ $l = \sqrt{\frac{\gamma \cos(\theta)r}{2\mu}} \cdot \sqrt{t}$

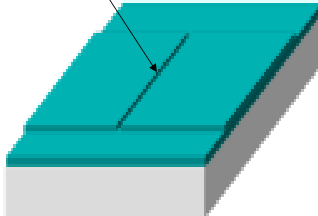
μ is the liquid viscosity

10

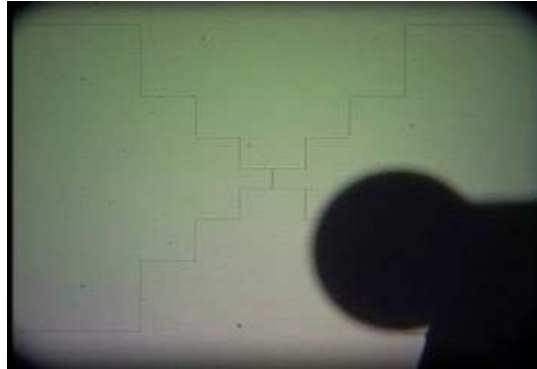


Capillary filling in open microchannel

Microchannel



Microchannel configuration



When a solution including microspheres ($6\mu\text{m}$ in diameter) is placed on microchannel, the solution is introduced by capillary action. The solution is continuously flowing due to the evaporation at the other side.

11

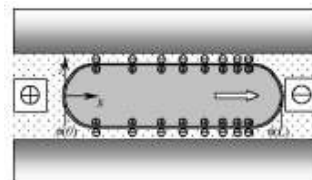
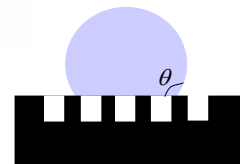


Fluid manipulation at small scale

- External pressure
 - Syringe pump
- Modify surface property
 - Micro-patterned surface
 - Surface coating
- Applying external electric field
 - Electro-wetting
- Change ion concentration



www.syringepump.com/



Electrically varied surface tension. Junhoon et al., *J. Microelectromech.*, 2000

12



Microchannel vs. nanochannel

- Size matters
 - EDL overlaps when channels shrink to nano size
 - Reduced electroosmotic mobility
 - Viscosity of liquids in nanochannels is substantially higher than in bulk
 - Surface effect is dominant
- For microchannels, a external voltage is required to generate large enough potential difference to drive flow
- The requirement for nanochannels is much lower due to its small size
- Filling length can be controlled by ion concentration

13



Zeta potential

- The potential induced by ions in liquid or charges on wall surface is called zeta potential ϕ
- Based on Debye-Hueckel approximation for charge density, the equilibrium zeta potential

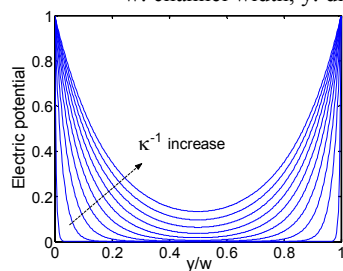
$$\nabla^2 \phi = -\rho_E / \epsilon \quad \Longrightarrow \quad \nabla^2 \phi = -\frac{2ce}{\epsilon_0 \epsilon} \sinh(-ze\phi / k_B T)$$

ρ_E : free charge density
 ϵ : permittivity

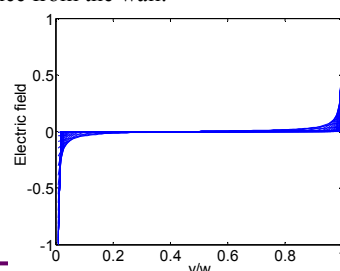
e : charge on a proton, z : valence of ion with concentration c

Assume $ze \ll k_B T$ $\nabla^2 \phi = \kappa^2 \phi$ where $\kappa = \sqrt{\frac{2cz^2 e^2}{\epsilon_0 \epsilon k_B T}}$ κ^{-1} : Debye length

w : channel width, y : distance from the wall.



Zeta potential distribution

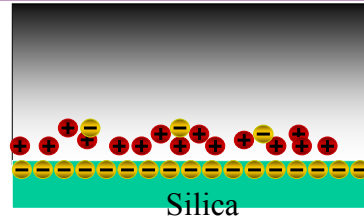
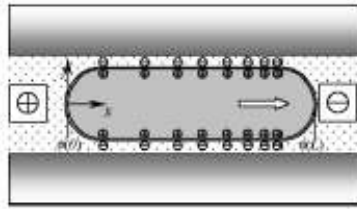


E field distribution

14



Electro-wetting theory



- Electrowetting: motion of electrolyte drop induced by an applied voltage between electrolyte and wall

$$\gamma_{dw} = \gamma_{dw}^0 - CV^2 / 2$$

where γ_{dw} is the total surface tension γ_{dw}^0 with only chemical components,

$C = \epsilon_m \epsilon_0 / h$ interface capacitance for a uniform dielectric of thickness h

V is the potential difference between electrolyte drop and wall

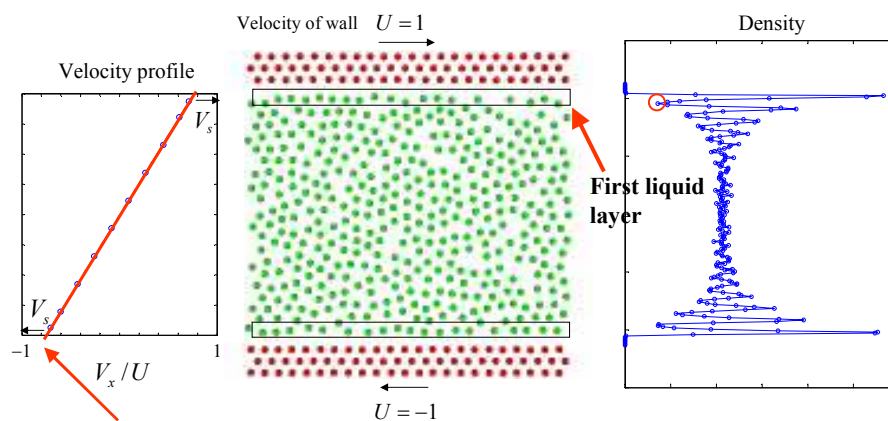
- The contact angle θ is given by the Young-Dupre equation as: $\gamma_{dw} = \gamma_w - \gamma_d \cos(\theta)$

$$\theta = \cos^{-1} \left(\frac{\gamma_w - \gamma_{dw}^0 + CV^2 / 2}{\gamma_d} \right)$$

15

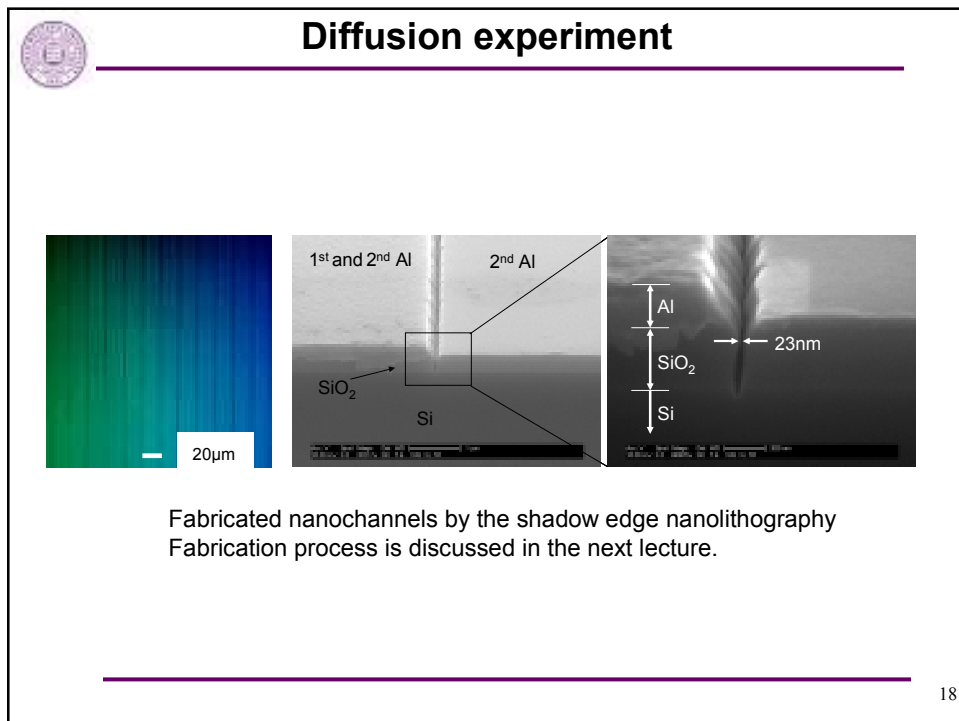
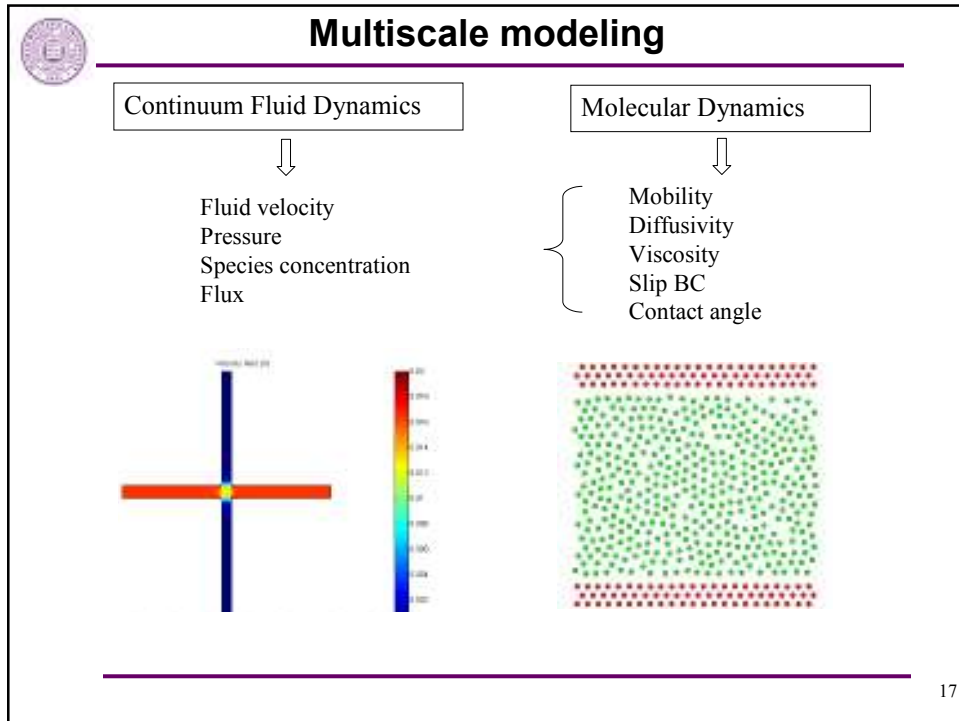


Dynamics of liquid flow in nanochannel



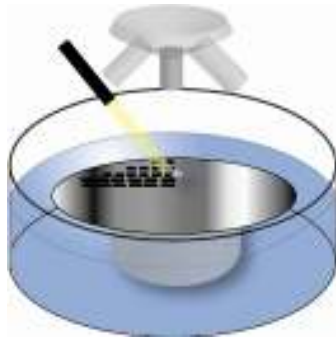
All slip occurs at the first liquid layer

16





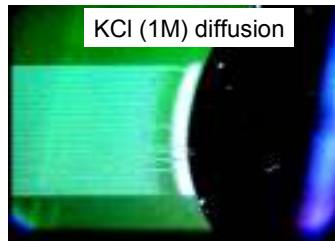
Diffusion experiment in open nanochannels



Nanochannel without solution



KCl (1M) diffusion

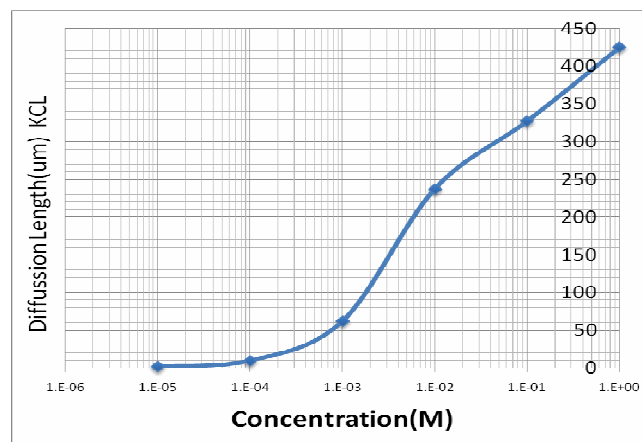


- Ionic solution is introduced at one side of the nanochannel.
- It is observed through microscope.
- The diffusion experiment is recorded by computer and analyzed by software.

19



Diffusion length at different ion concentration

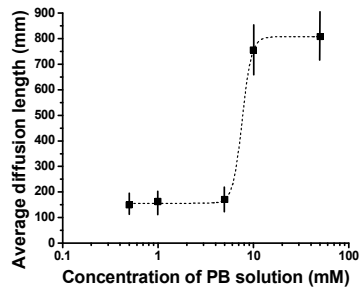


Diffusion length of KCl at different concentration

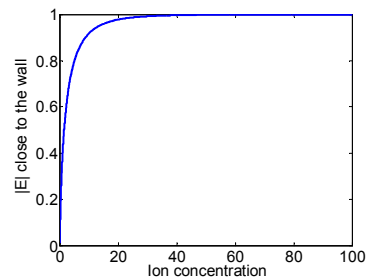
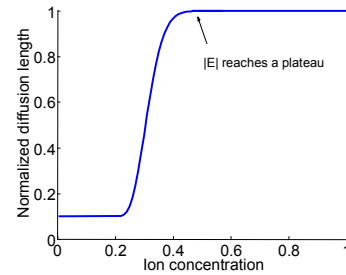
20



Diffusion length at different ion concentration



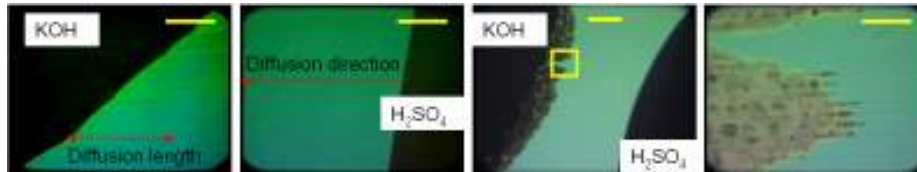
Three distinct regimes



21



Diffusion and reaction in nanochannels



- KOH solution on the left side and H_2SO_4 on the right.
- Depending on the charge of both solutions, a larger diffusion length is observed for H_2SO_4 .

22



Diffusion and reaction in nanochannels



KOH



H₂SO₄

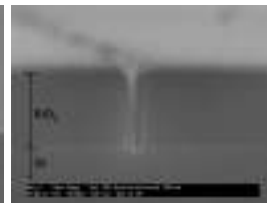
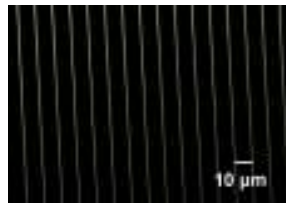
Salt generated during the reaction.

23



DNA chip using nanochannels

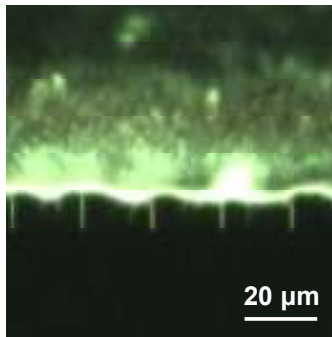
Array of Nanochannels



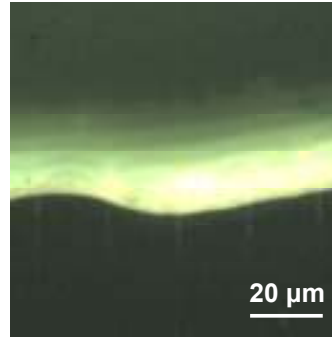
24



Diffusion Experiment in Nanochannels



λ -DNA molecules (1 $\mu\text{g/mL}$) treated with PicoGreen dye and TE buffer

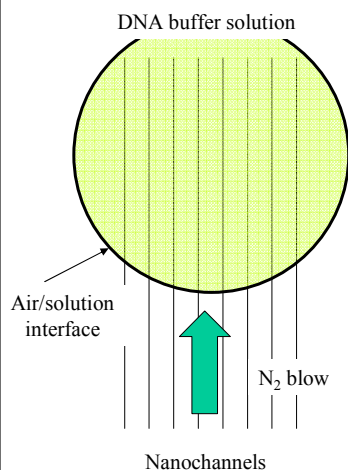


Fluorescein particles at 100 $\mu\text{g/mL}$ (0.3 mM)

25




DNA Fluorescence Images


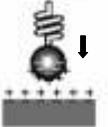



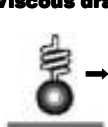


100 pg/mL DNA concentration (1/10000 X reagent)
(about 20,000 DNA molecules in $\sim 4 \mu\text{L}$ drop)

Since DNA is negatively charged, it is not introduced by capillary action in nanochannels.
External pressure was used for introducing DNA.


26

 **Summary of physics involved in two lectures**

<p>van der Waals</p>  $F(D) = \frac{AR}{12D^2}$	<p>Electrostatic</p>  $F(D) = \frac{4\pi R \lambda \sigma_R \sigma_S}{\epsilon} e^{-D/\lambda}$
<p>Brush</p>  $F(D) = \frac{50LkT}{s^2} e^{-2\alpha D}$ <p>$0.2 = 0.2L = 0.8$</p>	<p>Dielectrophoretic</p>  $F(D) \approx \Gamma \cdot \epsilon' \operatorname{Re}\{K_f\} \nabla(E^2) \propto \frac{1}{D^2}$
<p>Capillary force</p>  $F = 4\pi R \gamma_L \cos \theta$	<p>Viscous drag</p>  $F(D) = 6\pi\mu R \dot{\gamma} F_{wall}^* D$

Expanded/revised from Heinz and Hoh, *Trends Biotechnology*, 1999

27



**Size-exclusive capture
using nano needles
(Fishing DNA in fluid)**

28



Reference

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